

New MAC Constructions from (Tweakable) Block Ciphers

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Outline

Context

Block Cipher Based Constructions

Tweakable Block Cipher Based Constructions

Security of Truncated MACs

A word about the proofs

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A word about the proofs

Nonce-Based Message Authentication Codes


 (N, M, T)


$$T = \text{MAC}_K(N, M)$$

$$\text{MAC}_K(N, M) = T ?$$

Security Definition

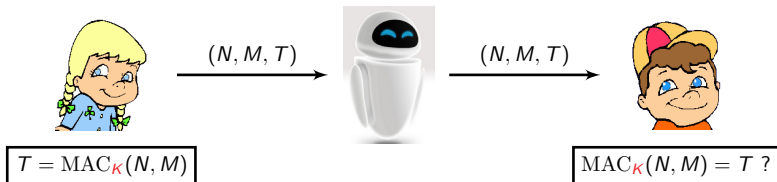
The adversary is allowed

- q_m MAC queries $T = \text{MAC}_K(N, M)$
- q_v verification queries (forgery attempts) (N', M', T')

and is successful if one of the verification queries (N', M', T') passes and no previous MAC query (N', M') returned T' .

The adversary is said **nonce-respecting** if it does not repeat nonces in MAC queries.

Nonce-Based Message Authentication Codes



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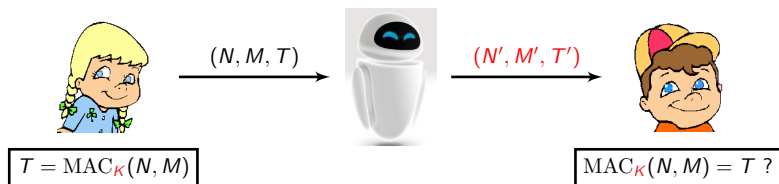
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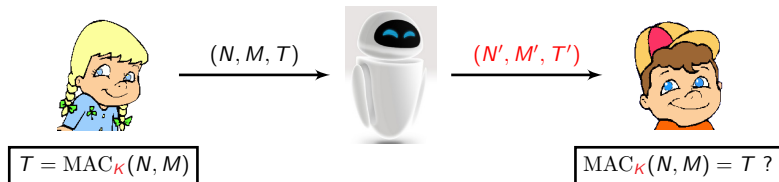
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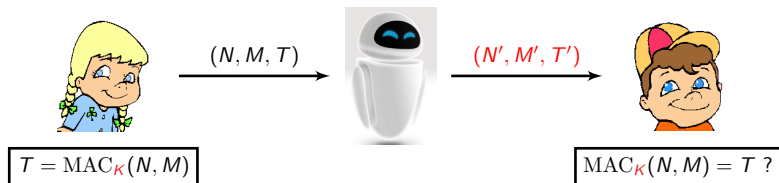
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Deterministic Message Authentication Codes


 (M, T)


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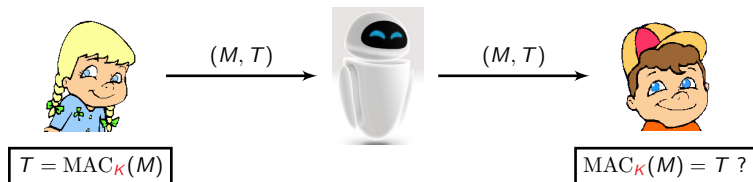
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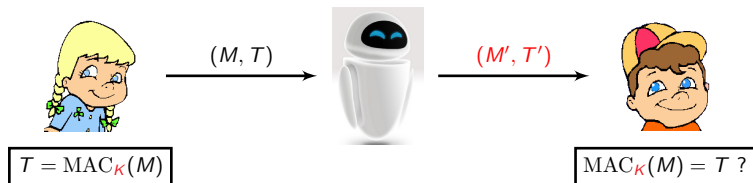
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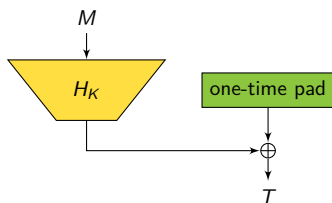
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Wegman-Carter MACs [GMS74, WC81]



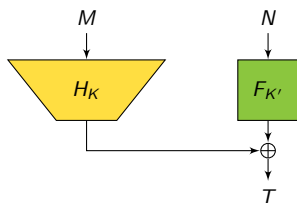
- based on an ε -almost xor-universal (ε -AXU) hash function H :

$$\forall M \neq M', \forall Y, \Pr[K \leftarrow_{\$} \mathcal{K} : H_K(M) \oplus H_K(M') = Y] \leq \varepsilon$$

- in practice, OTPs are replaced by a PRF applied to a **nonce** N
- H usually based on polynomial evaluation (GCM, Poly1305)
- “optimal” security:

$$\mathbf{Adv}_{\text{WC}}^{\text{MAC}}(q_m, q_v) \leq \varepsilon q_v + \mathbf{Adv}_F^{\text{PRF}}(q_m + q_v)$$

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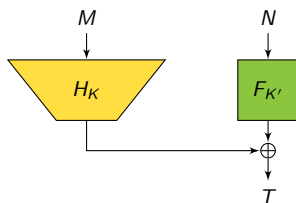
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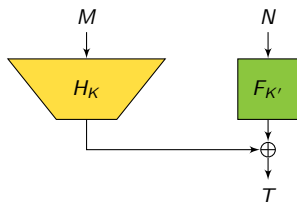
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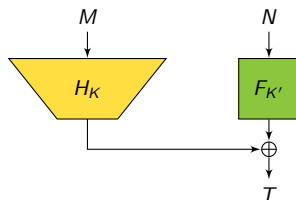
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The Nonce-Misuse Problem (1/2)

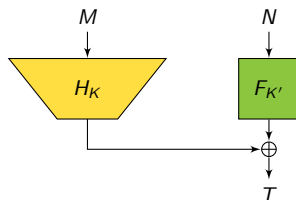


- Wegman-Carter MACs are brittle: a single **nonce repetition** can completely break security [Jou06, HP08]
- esp. for **polynomial-based** hashing, i.e., $H_K(M) = P_M(K)$:

$$\begin{cases} P_M(K) \oplus F_{K'}(N) = T \\ P_{M'}(K) \oplus F_{K'}(N) = T' \end{cases} \Rightarrow P_M(K) \oplus P_{M'}(K) = T \oplus T'$$

- solution: extra PRF call (in fact, OK to use a PRP here)

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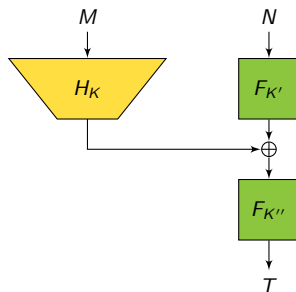


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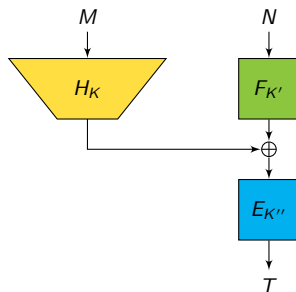


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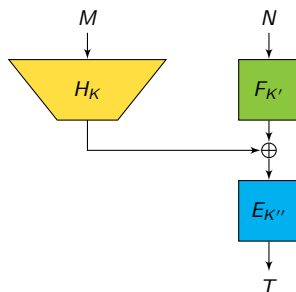


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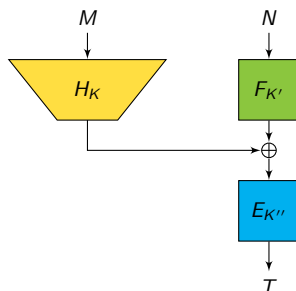
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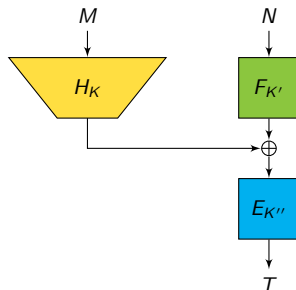
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- BUT security drops to the birthday bound when a nonce is used twice ;
- same problem when implementing F from a Block Cipher ;
- too simple mixing of the nonce and the hash of the message...

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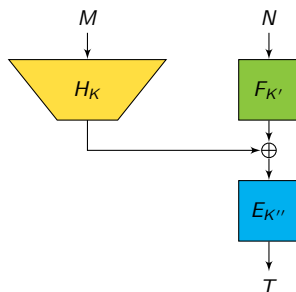
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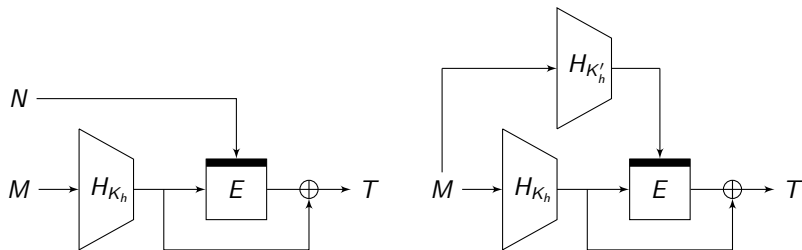
Block Cipher Based Constructions

Tweakable Block Cipher Based Constructions

Security of Truncated MACs

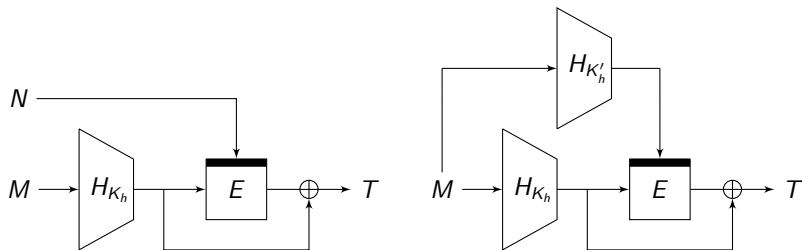
A word about the proofs

Our BC Based MACs



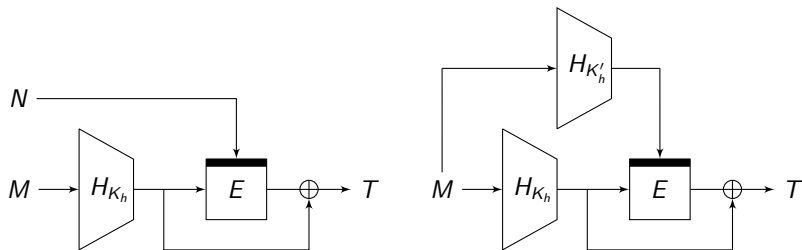
- Dubbed the HENK (*Hash-then-Encrypt with Nonce as Key*) and HEHK (*Hash-then-Encrypt with Hash as Key*) constructions.
- Based on a BC E and a ε -AXU and uniform hash function H .
- Efficient: 1 call to the BC and 1 call (2 for HEHK) to H .
- Provably secure in the Ideal Cipher Model.

Our BC Based MACs



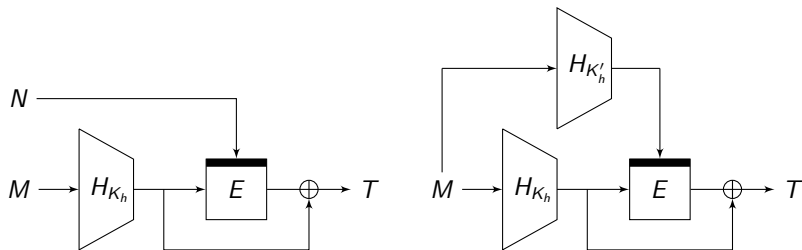
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The HENK construction and its randomized variant HERK

- probability of forgery for a (μ, q_e, q_m, q_v) -adversary is lower than

$$(5\mu + n - 2)\varepsilon q + \frac{q}{2^n - \mu - q} + \left(\frac{q}{2^n - q}\right)^{n+1},$$

where $q = \max(q_e, q_m, q_v)$ (more accurate bound in the paper).

- Randomized variant is dubbed the HERK construction (*Hash-then-Encrypt with Random Key*).
- probability of forgery for a (q_e, q_m, q_v) -adversary is then lower than

$$(6n - 2)\varepsilon q + \frac{q}{2^n - n - q} + \left(\frac{q}{2^n - q}\right)^{n+1} + \left(\frac{q}{|\mathcal{K}|}\right)^n \frac{q}{2^n}.$$

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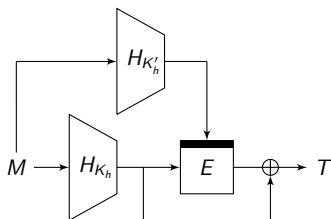
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The HEHK construction



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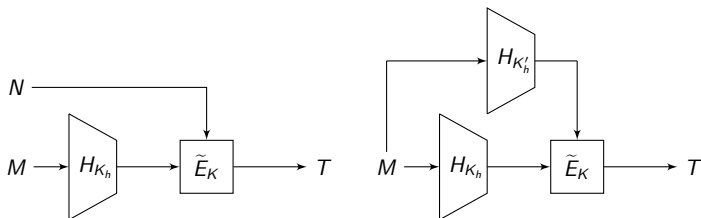
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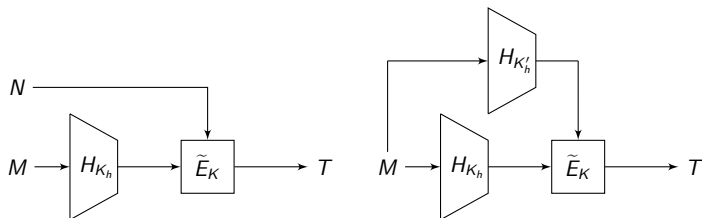
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Our TBC-based MAC constructions



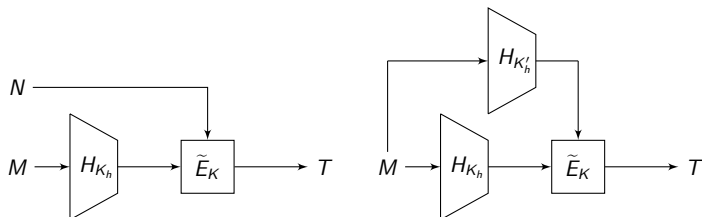
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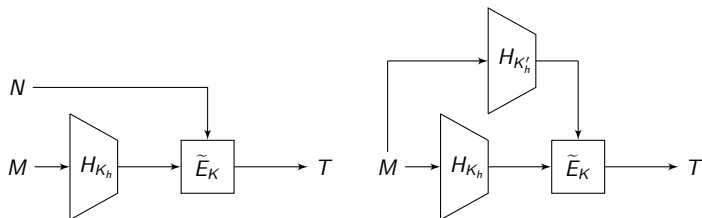
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The HENT construction and its randomized variant HERT

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$$\mathbf{Adv}_{\tilde{E}}^{\text{TPRP}}(2q) + (3\mu - 2)q\varepsilon + \frac{q}{2^n - \mu}$$

where $q = \max(q_e, q, q_v)$ (better bound in the paper).

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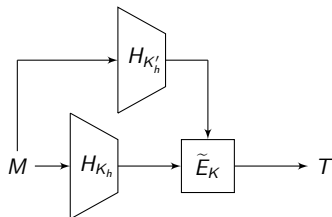
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The HEHT construction



Probability of forgery for a (q_m, q_v) -adversary is lower than

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A word about the proofs

What about truncated variations of our constructions ?

Our constructions compose well with truncation.

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E.g., if one takes the first s bits of the outputs of the HEHT construction, the probability of forgery of a (q_m, q_v) -adversary is lower than

$$\mathbf{Adv}_{\tilde{E}}^{\text{TPRP}}(A') + 2\varepsilon^2 q_m^2 + 2^{n-s} \varepsilon^2 q_m q_v + \frac{2^{n-s} q_v}{2^n - q_m}.$$

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Proof strategy

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- H-coefficients technique [Pat08, CS14] (good/bad transcripts).
- No “Ideal world” in the MAC security notions.
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Bad transcripts for HENT (1/2)

- In the ideal world, the verification oracle always rejects \Rightarrow avoid situations where an adversary would have won in the real world:
 - happens if there exists a MAC query $(N_i, M_i, T_i) \in \tau_m$ and a verification query $(N'_j, M'_j, T'_j, b_j) \in \tau_v$ such that

$$\begin{cases} N_i = N'_j \\ T_i = T'_j \\ H_{K_h}(M_i) = H_{K_h}(M'_j), \end{cases}$$

- BUT only with probability lower than $\mu q_v \varepsilon$.

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- Avoid collisions which make the transcript incompatible with a permutation:
 - can happen if there exists two distinct MAC queries (N, M, T) and (N', M', T') such that $N = N'$ and either $H_{K_h}(M) = H_{K_h}(M')$ or $T = T'$.
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Good transcripts for HENT

Fix any good transcript $\tau = (\tau_m, \tau_v, K_h)$

- r is the number of distinct tweaks used in τ_m , and for $i = 1, \dots, r$, q_i is the number of occurrences of the i -th tweak in τ_m ;
- then

$$\Pr[X_{\text{id}} = \tau] = \frac{1}{|\mathcal{K}_h| \cdot 2^{nq_m}},$$

$$\Pr[X_{\text{re}} = \tau] \geq \frac{1}{\prod_{i=1}^r (2^n)^{q_i}} \left(1 - \frac{q_v}{2^n - \mu}\right),$$

- and

$$\Pr[X_{\text{re}} = \tau] / \Pr[X_{\text{id}} = \tau] \geq 1 - \frac{q_v}{2^n - \mu}.$$

Conclusion

- We propose efficient and provably secure MAC constructions based on a BC or a TBC and ε -AXU and uniform hash function:
- two Nonce-based MACs (HENK and HENT) whose security degrades linearly as the number of nonce reuses grows,
- two Randomized MACs (HERK and HERT) based on the previous ones,
- and two Deterministic MACs with security up to roughly ε^{-1} .
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Thanks for your attention !

References I



Shan Chen and John Steinberger. Tight Security Bounds for Key-Alternating Ciphers. In Phong Q. Nguyen and Elisabeth Oswald, editors, *Advances in Cryptology - EUROCRYPT 2014*, volume 8441 of *LNCS*, pages 327–350. Springer, 2014. Full version available at <http://eprint.iacr.org/2013/222>.



Edgar N. Gilbert, F. Jessie MacWilliams, and Neil J. A. Sloane. Codes which detect deception. *Bell System Technical Journal*, 53(3):405–424, 1974.



Helena Handschuh and Bart Preneel. Key-Recovery Attacks on Universal Hash Function Based MAC Algorithms. In David Wagner, editor, *Advances in Cryptology - CRYPTO 2008*, volume 5157 of *LNCS*, pages 144–161. Springer, 2008.



Antoine Joux. Authentication Failures in NIST Version of GCM. Comments submitted to NIST Modes of Operation Process, 2006. Available at http://csrc.nist.gov/groups/ST/toolkit/BCM/documents/comments/800-38_Series-Drafts/GCM/Joux_comments.pdf.

References II



Jacques Patarin. The “Coefficients H” Technique. In Roberto Maria Avanzi, Liam Keliher, and Francesco Sica, editors, *Selected Areas in Cryptography - SAC 2008*, volume 5381 of *LNCS*, pages 328–345. Springer, 2008.



Mark N. Wegman and Larry Carter. New Hash Functions and Their Use in Authentication and Set Equality. *J. Comput. Syst. Sci.*, 22(3):265–279, 1981.